

HW #4

Slow-Start Analysis:

The attached figure shows the progression of the sliding window protocol under ideal conditions. It is assumed that the round-trip time is fixed at s :

$$s = \text{transp} + \text{transa} + 2 * (\text{proc} + \text{prop})$$

Assume that W_{max} is even and that $s = W_{\text{max}} * \text{transp}$

Let

$$a = \text{transp}$$

$$b = \text{transa}$$

$$s = a + b$$

$$W_{\text{max}} = (a + b)/a = 1 + b/a$$

The efficiency is simply a measure of the ratio of 'active time' during new packet transmission is taking place divided by the total elapsed time. The following 'table' illustrates the progression for slow-start and congestion avoidance from $W=1$ to $W=W_{\text{max}}$ as shown in the diagram:

<u>Active Time</u>	<u>Elapsed Time</u>	<u>Next Window</u>
a	$s = a + b$	2
2a	$s = a + b$	4
.....	$s = a + b$	
$W_{\text{max}}/4 * a$	$s = a + b$	$W_{\text{max}}/2$
$W_{\text{max}}/2 * a$	$s = a + b$	$W_{\text{max}}/2 + 1$
$(W_{\text{max}}/2 + 1) * a$	$s = a + b$	$W_{\text{max}}/2 + 2$
.....	$s = a + b$	
$(W_{\text{max}} - 1) * a$	$s = a + b$	W_{max}
$W_{\text{max}} * a$	$s = a + b$	W_{max}

$$\text{Total Active Time} = a * \sum 2^w + a * \sum w$$

The limits of the first sum are: $w = 1$ to $w = \log\text{-base-2 } W_{\text{max}}/2$

The limits of the second sum are: $w = W_{\text{max}}/2 + 1$ to $w = W_{\text{max}}$

$$\text{Total Elapsed Time} = (a + b) \log\text{-base-2 } W_{\text{max}}/2 + (a + b) W_{\text{max}}/2$$

The final solution can be simplified as desired.

