

# EECE 2150 - Circuits and Signals: Biomedical Applications Fall 2018, Quiz 6

Prof. Charles A. DiMarzio

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Student Name: \_\_\_\_\_

Consider the circuit in the figure. This is a simple example of a Marx generator, which can be used to generate high-voltage pulses.

All capacitors are  $0.1 \mu\text{F}$ , all resistors labelled  $R_1$  are  $1 \text{ k}\Omega$ , and the load resistor is  $R_L = 1 \Omega$ . The switches are open for a long time, and then closed at  $t = 0$ .

1. What is the capacitance of each series combination of two capacitors?

$$C_{series} = \text{_____} \mu\text{F}.$$

2. The switches are opened for a long time, so that the circuit has reached steady state. What is the voltage across each series pair of capacitors?

$$V_{left}(0^-) = \text{_____} \text{ Volts.}$$

$$V_{right}(0^-) = \text{_____} \text{ Volts.}$$

3. How much energy is stored in the capacitors in total? Hint: Do this for one capacitor at a time.

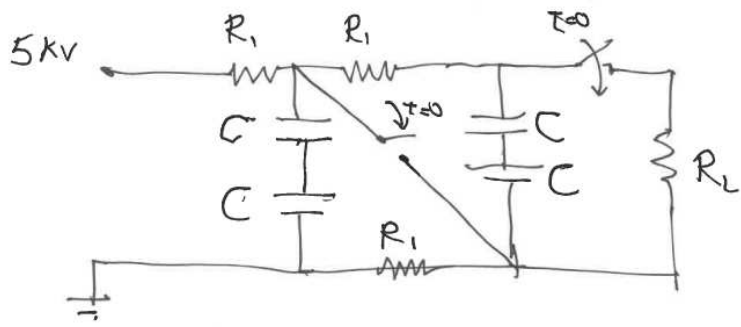
$$W(0^-) = \text{_____} \text{ Joules.}$$

4. Then the switches are closed at time,  $t = 0$ . What is the voltage just after the switches are closed?

$$V(0^+) = \text{_____} \text{ Volts.}$$

5. What is the time constant of the circuit with the switches closed? Use appropriate approximations to make it an easy calculation.

$\tau =$  \_\_\_\_\_ Sec.



1. Series Capacitors;  $1/C_{series} = 1/C_1 + 1/C_2 = 2/C$

$$C_{series} = C/2 = 0.05 \mu\text{F}.$$

2.  $V(0^-) = 5 \text{ kV}$  for both.

3. Each capacitor sees half the voltage, so the energy in one is

$$W_1 = \frac{1}{2}C \left(\frac{V}{2}\right)^2 = \frac{1}{2} \times 0.1 \times 10^{-6} \text{ F} \times (2500 \text{ V})^2$$

In total

$$W = 4W_1 = 4 \times \frac{1}{2} \times 0.1 \times 10^{-6} \text{ F} \times (2500 \text{ V})^2 = 1.25 \text{ J}$$

4. Now capacitors are stacked all in series;  $10 \text{ kV}$ .

5. The total capacitance is the series combination of all 4, so

$$C_{after} = C/4 = 0.025 \mu\text{F}$$

$$RC = 0.025 \mu\text{F} \times 1 \Omega = 25 \text{ ns}.$$