# Northeastern University College of Engineering 

## EECE2150 Circuits and Signals: Biomedical Applications

Final Exam
April 29, 2015

Name: $\qquad$Show all work leading to the solutions.
Place a box or circle around all final results.
$\square$ You may use your calculators, but are not permitted to share them.
$\square$ Turn off your cell phone, and remove it from your table.
$\square$ This test contains 5 problems and one 5-point extra credit problem. If you need more space, you can write on the back of the pages.

1. (20 pts) In the circuit below the $g_{m}=0.03 \frac{A}{V}$.
a. Write a set of node-voltage equations and an equation of constraint expressing $v_{\pi}$ in terms of your node voltages.
b. Put your equations in standard form

$$
\left[\begin{array}{ll}
A_{11} & A_{12} \\
A_{21} & A_{22}
\end{array}\right]\left[\begin{array}{l}
V_{A} \\
V_{B}
\end{array}\right]=\left[\begin{array}{l}
d_{1} \\
d_{2}
\end{array}\right]
$$

c. Find the solution for $v_{o}$ OR write the MATLAB commands you would use to find $v_{o}$.

2. (20 pts) The op amp in the circuit below can be assumed to be ideal. If $v_{A}=4 \mathrm{~V}$ and $v_{B}=1 \mathrm{~V}$ find the output voltage $v_{o}$.

3. (20 pts) In the circuit shown, the switch is thrown as shown at time $t=0$.
a. Convert the circuit to the left of points (a)-(b) to a Thevenin voltage source.
b. What is the equivalent capacitance of the two capacitors?
c. Find an expression for the voltage across the capacitors as a function of time $V_{C}(t)$.
d. What is $V_{C}$ at $=4 \mathrm{~ms}$ ?

4. (20 pts) In the circuit below $v_{s}(t)=3 \cos 8000 t \mathrm{~V}$
a. Find the steady-state expression for $i_{o}(t)$
b. Find the real power dissipated in the circuit (or equivalently the real power supplied by the source).

5. (20 pts) The following questions refer to the circuit shown.
a. Is the op am circuit shown below a low-pass or high-pass filter?
b. Assuming that the capacitor has a value $\mathrm{C}=10 \mu \mathrm{~F}$, select values of $\mathrm{R}_{1}$ and $\mathrm{R}_{2}$ to give a cutoff frequency of $\omega_{0}=1.0$ radians/s and a high-frequency gain $\left|\frac{V_{o}}{V_{s}}\right|=5$.
c. Assuming that you have a $V_{S}$ that has Fourier components as shown in the graph, sketch what you would expect the Fourier components of $\mathrm{V}_{\mathrm{o}}$ to be - i.e. make a plot similar to the one shown below for $\mathrm{V}_{\mathrm{o}}(\omega)$.



Extra Credit: (5 pts) Derive the frequency at which the transfer function $H(\omega)=V_{o} / V_{i}$ of the following circuit is equal to zero.


